

Key

TEACHER: \_\_\_\_\_

Alg 2 CC Regents June 1<sup>st</sup>

- even vs. odd
- ARAC
- ✓ ◦ SOAP

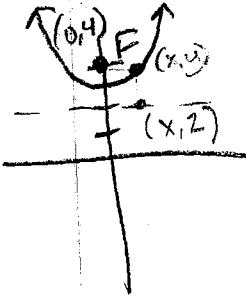
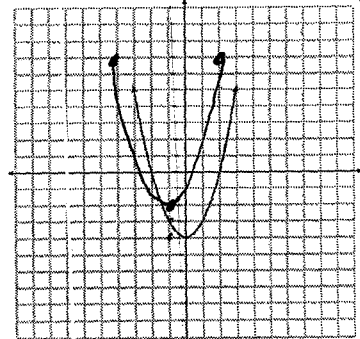
- alg. system
- ✓ ◦ Rat. eq'n

\*\*Formulas to know - Important things to remember\*\*

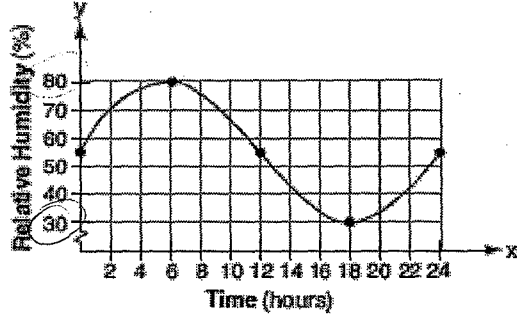
div. /  
asympt.

✓  $x^4 - 3x^2 - 10 = 0$

# REVIEW # 1

	Question/WORK	ANSWER
1.	<p>The minimum point on the graph of the equation <math>y = f(x)</math> is <math>(-1, -3)</math>. What is the minimum point on the graph of the equation <math>y = f(x) + 5</math>?</p> <p> <input checked="" type="radio"/> 1) <math>(-1, 2)</math>  <input type="radio"/> 2) <math>(-1, -8)</math>  <input type="radio"/> 3) <math>(4, -3)</math>  <input type="radio"/> 4) <math>(-6, -3)</math> </p>	<p>(1)</p>
2.	<p>Which transformation of <math>y = f(x)</math> moves the graph 7 units to the <u>left</u> and 3 units <u>down</u>?</p> <p> <input checked="" type="radio"/> 1) <math>y = f(x + 7) - 3</math>  <input type="radio"/> 2) <math>y = f(x + 7) + 3</math>  <input type="radio"/> 3) <math>y = f(x - 7) - 3</math>  <input type="radio"/> 4) <math>y = f(x - 7) + 3</math> </p>	<p>(1)</p>
3.	<p>Derive the equation of a parabola given the focus of <math>(0, 4)</math> and the directrix <math>y = 2</math>.</p>  $d = \sqrt{(x-0)^2 + (y-4)^2} = d = \sqrt{(x-x)^2 + (y-2)^2}$ $\sqrt{x^2 + (y-4)^2} = \sqrt{(y-2)^2}$ $x^2 + (y-4)^2 = (y-2)^2$ $x^2 + y^2 - 8y + 16 = y^2 - 4y + 4$ $x^2 - 4y + 12 = -4y$	
4.	<p>The function <math>f(x)</math> is graphed on the set of axes below. On the same set of axes, graph <math>f(x + 1) + 2</math>.</p> <p>left 1 up 2</p> 	$x^2 - 8y + 12 = -4y$ $\frac{x^2 - 8y + 12}{-4} = \frac{-4y}{-4}$ $y = -\frac{1}{4}x^2 + 2y - 3$ $\frac{-2y}{-2y} = \frac{-2y}{-2y}$ $-y = -\frac{1}{4}x^2 - 3$ $y = \frac{1}{4}x^2 + 3$

5. A meteorologist drew the accompanying graph to show the changes in relative humidity during a 24-hour period in New York City.



What is the range of this set of data?

- 1)  $0 \leq y \leq 24$
- 2)  $0 \leq x \leq 24$
- 3)  $30 \leq y \leq 80$
- 4)  $30 \leq x \leq 80$

(3)

6. Factor:  $6a^2 + 7ax - 3x^2$

$ac = -18$   
 $b = 7$

$9 < -2$

$$6a^2 + 9ax - 2ax - 3x^2$$

$$3a(2a + 3x) - x(2a + 3x)$$

$$(3a - x)(2a + 3x)$$

7. Solve the system:

$$6x - 2y - 4z = -8$$

$$3x - 5y + 5z = -14$$

$$-6 = 3(x + y - 5z = 6)$$

$$3x - 5y + 5z = -14$$

$$+ \quad -3x - 3y + 15z = -18$$


---


$$-8y + 20z = -32$$
  

$$6x - 2y - 4z = -8$$

$$+ \quad -6x - 6y + 30z = -36$$


---


$$-8y + 26z = -44$$

$$-8y + 20z = -32$$

$$-(-8y + 26z = -44)$$


---


$$-8y + 20z = -32$$

$$+ \quad 8y - 26z = 44$$


---


$$-6z = 12$$

$$z = -2$$

$$x = -3$$

$$y = -1$$

$$z = -2$$

$$x - 1 - 5(-2) = 6$$

$$x - 1 + 10 = 6$$

$$x + 9 = 6$$

$$x = -3$$

$$-8y + 20(-2) = -32$$

$$-8y - 40 = -32$$

$$-8y = 8$$

$$y = -1$$

8. Multiply  $(2x^3 + 1)(5x^2 + 4)$  and write your result in simplest form.

$$10x^5 + 8x^3 + 5x^2 + 4$$

9. Write an equation of the line, in point-slope form, whose slope is 5 and passes through  $(-5, 3)$ .

$$y - 3 = 5(x + 5)$$

10. Find the slope of the line that passes through the points  $(5, -2)$  and  $(20, 4)$ .

$$m = \frac{4 - (-2)}{20 - 5} = \frac{6}{15} = \frac{2}{5}$$

11. Find the inverse of  $f(x) = (x - 5)^3 - 1$

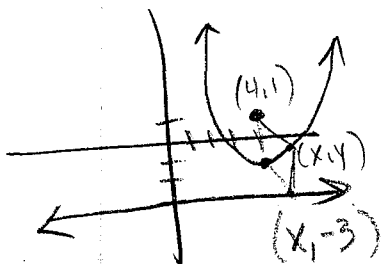
$$x = (y - 5)^3 - 1$$
$$\sqrt[3]{x + 1} = \sqrt[3]{(y - 5)^3}$$
$$\sqrt[3]{x + 1} = y - 5$$
$$+ 5$$

$$f^{-1}(x) = \sqrt[3]{x + 1} + 5$$

# REVIEW # 2

	Question/WORK	ANSWER
1.	<p>Solve the system: <math>\begin{cases} x-2y+z=-11 \\ 3x+2y-z=7 \\ -x+2y+4z=-9 \end{cases}</math></p> $4x = -4$ $x = -1$ $5z = -20$ $z = -4$ $-1 - 2y - 4 = -11$ $\begin{array}{r} -2y - 5 = -11 \\ +5 \quad +5 \\ \hline -2y = -6 \\ y = 3 \end{array}$	$x = -1$ $y = 3$ $z = -4$
2.	<p>Write, in POINT-SLOPE form, the equation of the line that passes through points <math>(-1, 2)</math> and <math>(7, -3)</math>.</p> $m = \frac{2 - (-3)}{-1 - 7} = \frac{5}{-8}$ $y - 2 = -\frac{5}{8}(x + 1)$	

3. Use the distance formula to write the equation of the parabola that is the collection of all points equidistant from (4, 1) and y = -3.



$$\sqrt{(x-4)^2 + (y-1)^2} = \sqrt{(x-x)^2 + (y+3)^2}$$

$$x^2 - 8x + 16 + y^2 - 2y + 1 = x^2 + 6y + 9$$

$$x^2 - 8x + 8 = 6y$$

$$y = \frac{1}{6}x^2 - x + \frac{4}{3}$$

OR  $V(4, 1) \quad p = 2$

$$y = \frac{1}{8}(x-4)^2 - 1$$

$$y = \frac{1}{8}(x^2 - 8x + 16) - 1$$

$$y = \frac{1}{8}x^2 - x + 2 - 1$$

$$y = \frac{1}{8}x^2 - x + 1$$

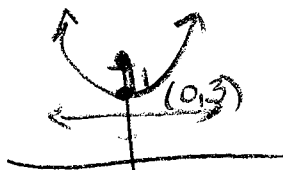
4. Which equation represents a parabola with a focus of (0, 4) and a directrix of y = 2?

(1)  $y = x^2 + 3$

(2)  $y = -x^2 + 1$

(3)  $y = \frac{1}{2}x^2 + 3$

(4)  $y = \frac{1}{4}x^2 + 3$



$$y = \frac{1}{4p}(x-h)^2 + k$$

$$y = \frac{1}{4(1)}(x-0)^2 + 3$$

$$y = \frac{1}{4}x^2 + 3$$

5. Find the axis of symmetry of the parabola whose equation is  $f(x) = -2x^2 - 8x + 5$ .

$$x = \frac{-b}{2a} = \frac{8}{2(-2)} = -2$$

$$x = -2$$

6. Find the vertex of the parabola whose equation is  $f(x) = -2x^2 - 8x + 5$ .

$$f(x) = -2x^2 - 8x + 5$$

$$-2(-2)^2 - 8(-2) + 5 = 5$$

$$-8 + 16 + 5 = 13$$

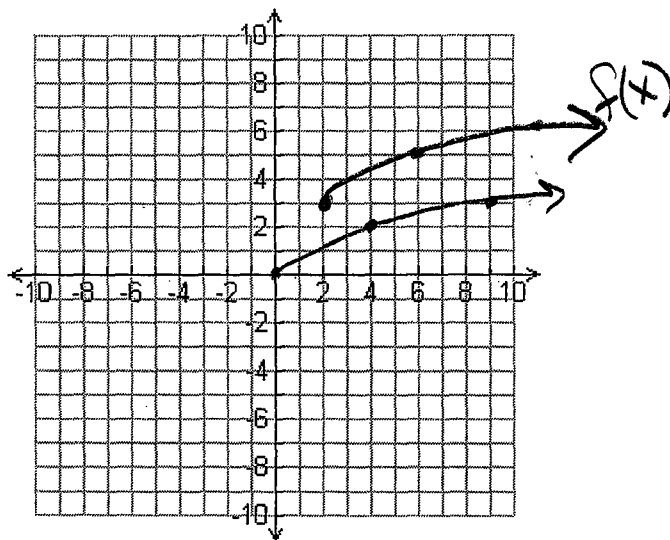
$$(-2, 13)$$

7. Find the y-intercept of the parabola whose equation is  $f(x) = -2x^2 - 8x + 5$ .

(0, 5)

8. Graph  $f(x) = \sqrt{x-2} + 3$ , without a calculator (using transformations). right 2, up 3

$g(x) = \sqrt{x}$



9. State the domain of  $f(x) = \sqrt{x-2} + 3$ .

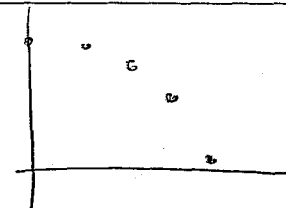
$x \geq 2$

10. State the range of  $f(x) = \sqrt{x-2} + 3$ .

$y \geq 3$

11. The table below shows the heights,  $y$  of a competitive water skier  $x$  seconds after jumping off a ramp. **Use your calculator** to write a function that model the height of the water-skier over time. When is the water-skier 5 feet above the water? How long is she in the air?

Time (seconds), $x$	0	.25	.75	1	1.1
Height (feet), $y$	22	22.5	17.5	12	9.24



$y = -16x^2 + 60x + 22$

$x = 1.24$  SECS.

$x = 1.375$  SECS.

# REVIEW # 3

	Questions/WORK	ANSWER
1.	<p>The relationship between <math>t</math>, a student's test scores, and <math>d</math>, the student's success in college, is modeled by the equation <math>d = 0.48t + 75.2</math>. Based on this linear regression model, the correlation coefficient could be</p> <p>1) between <math>-1</math> and <math>0</math>                  2) between <math>0</math> and <math>1</math>                  3) equal to <math>-1</math>                  4) equal to <math>0</math></p> <p style="text-align: right;">"r"</p>	(2)
2.	<p>Factor: <math>6a^2 + 9ab - 3b - 2a</math></p> <p style="font-size: 1.5em;"><math>3a(2a + 3b) - 1(3b + 2a)</math></p> <p style="font-size: 1.5em;"><math>(3a - 1)(2a + 3b)</math></p>	
3.	<p>Solve <math>2x^2 - 12x + 4 = 0</math> by completing the square, expressing the result in simplest radical form.</p> <p style="font-size: 1.5em;"><math>x^2 - 6x + 2 = 0</math></p> <p style="font-size: 1.5em;"><math>x^2 - 6x + 9 = -2 + 9</math></p> <p style="font-size: 1.5em;"><math>(x - 3)^2 = 7</math></p> <p style="font-size: 1.5em;"><math>x - 3 = \pm\sqrt{7}</math></p> <div style="border: 1px solid black; padding: 5px; display: inline-block; font-size: 1.5em;"> <math>x = 3 \pm \sqrt{7}</math> </div>	
4.	<p>The conjugate of <math>7 - 5i</math> is</p> <p>1) <math>-7 - 5i</math>                  2) <math>-7 + 5i</math>                  3) <math>7 - 5i</math>                  4) <math>7 + 5i</math></p>	(4)
5.	<p>Determine the value of <math>n</math> in simplest form: <math>i^{13} + i^{18} + i^{31} + n = 0</math></p> <p style="font-size: 1.5em;"><math>i^1 \quad i^2 \quad i^3</math></p> <p style="font-size: 1.5em;"><math>i - 1 + -i + n = 0</math></p>	$n = 1$

Why removed?

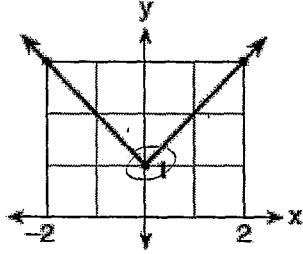


6. Multiply  $x + yi$  by its conjugate, and express the product in simplest form.

$$(x + yi)(x - yi)$$
$$x^2 - y^2 \underset{= -1}{i^2}$$

$$x^2 + y^2$$

7. Which equation represents the function shown in the accompanying graph?



$$(1)$$

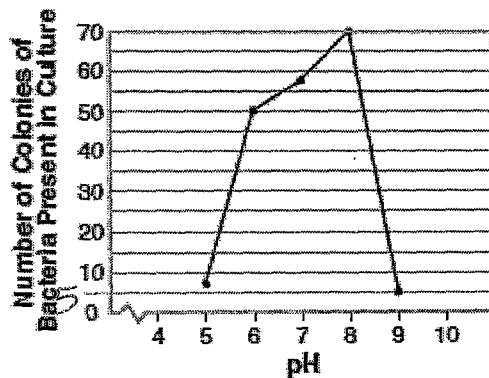
1)  $f(x) = |x| + 1$

2)  $f(x) = |x| - 1$

3)  $f(x) = |x + 1|$

4)  $f(x) = |x - 1|$

8. The accompanying graph illustrates the presence of a certain strain of bacteria at various pH levels.



What is the range of this set of data?

$$5 \leq y \leq 70$$

$$[5, 70]$$

9.

What are the coordinates of the center of a circle whose equation is

$$x^2 + y^2 - 16x + 6y + 53 = 0?$$

1)  $(-8, -3)$

2)  $(-8, 3)$

3)  $(8, -3)$

4)  $(8, 3)$

$$x^2 - 16x + 9 + y^2 + 6y + 9 = -53 + 64 + 9$$

$$(x-8)^2 - (y+3)^2 = 20$$

$$(8, 3)$$

(3)

10.

1. Solve the system of equations:

$$x = 3$$

$$5x + 4y = -9$$

$$-x + 4y - 2z = -25$$

$$\rightarrow 5(3) + 4y = -9$$

$$15 + 4y = -9$$

$$4y = -24$$

$$y = -6$$

$$x = 3$$

$$y = -6$$

$$z = -1$$

$$-3 + 4(-6) - 2z = -25$$

$$-3 - 24 - 2z = -25$$

$$-27 - 2z = -25$$

$$+27$$

$$+27$$

$$-2z = 2$$

$$z = -1$$

REVIEW # 4

	Question/WORK	ANSWER
1.	<p>In an electrical circuit, the voltage, <math>E</math>, in volts, the current, <math>I</math>, in amps, and the opposition to the flow of current, called impedance, <math>Z</math>, in ohms, are related by the equation <math>E = IZ</math>. A circuit has a current of <math>(3 + i)</math> amps and an impedance of <math>(-2 + i)</math> ohms. Determine the voltage in <math>a + bi</math> form.</p> <p><math>E = IZ</math>  <math>E = (3+i)(-2+i) = -6 + 3i - 2i + i^2</math>  <math>-6 + i - 1 \Rightarrow</math></p>	<p><math>-7 + i</math></p>
<p>2. why removed?</p>	<p>Simplify: <math>\sqrt{50x^3y^2}</math></p> <p><math>\sqrt{25} \sqrt{2} = 5\sqrt{2}</math>      <math>\sqrt{x^3} = \sqrt{x^2} \sqrt{x} = x\sqrt{x}</math>      <math>\sqrt{y^2} = y</math></p>	<p><math>5xy\sqrt{2x}</math></p>
3.	<p>Solve the system:</p> $\begin{array}{r} -3x - y + 6z = -17 \\ -3x - 5y - 5z = 21 \\ -6x + y + 3z = -28 \end{array}$ <p><math>2(-3x - y + 6z = -17)</math>  <math>-6x - 2y + 12z = -34</math>  <math>-6x + y + 3z = -28</math>  <hr/> <math>4(-3y + 9z = -6)</math>  <math>3(4y + 11z = -38)</math></p> <p><math>-12y + 36z = -24</math>  <math>+ 12y + 33z = -114</math>  <hr/> <math>69z = -138</math>  <math>z = -2</math></p> <p><math>4y + 11(-2) = -38</math>  <math>4y - 22 = -38</math>  <math>4y = -16</math>  <math>y = -4</math></p> <p><math>-3x - 4 + 6(-2) = -17</math>  <math>-3x - 4 - 12 = -17</math>  <math>-3x - 16 = -17</math>  <math>-3x = -1</math>  <math>x = 3</math></p> <p><math>(3, -4, -2)</math></p>	<p><math>z = -2</math></p> <p><math>x = 3</math></p> <p><math>(3, -4, -2)</math></p>
4.	<p>Which equation has imaginary roots? <math>b^2 - 4ac</math></p> <p>1) <math>x^2 - 2x + 1 = 0</math> <math>(-2)^2 - 4(1)(1) = 4 - 4 = 0 \times</math>          2) <math>x^2 - 2x - 1 = 0</math> <math>(-2)^2 - 4(1)(-1) = 4 + 4 = 8 \times</math>          3) <math>x^2 - 2x + 5 = 0</math> <math>(-2)^2 - 4(1)(5) = 4 - 20 = -16 \checkmark</math>          4) <math>x^2 - 2x - 5 = 0</math> <math>(-2)^2 - 4(1)(-5) = 4 + 20 = 24 \times</math></p>	<p>(3)</p>

5. The data table below shows water temperatures at various depths in an ocean.

Water Depth (meters)	Temperature (y) (°C)
50	18
75	15
100	12
150	7
200	1

Write the linear regression equation for this set of data, rounding all values to the nearest thousandth. Using this equation, predict the temperature (°C), to the nearest integer, at a water depth of 255 meters.

$$y = -0.112x + 23.448$$

$$y = -0.112(255) + 23.448$$

$$= -5^{\circ}\text{C}$$

6. Factor:  $1 - x - x^2 + x^3$

$$x^3 - x^2 - x + 1$$

$$x^2(x-1) - 1(x-1)$$

$$(x^2 - 1)(x - 1)$$

~~DOTS~~

$$(x+1)(x-1)(x-1)$$

$$(x^2 - 1)(x - 1)$$

$$x^3 - x^2 - x + 1$$

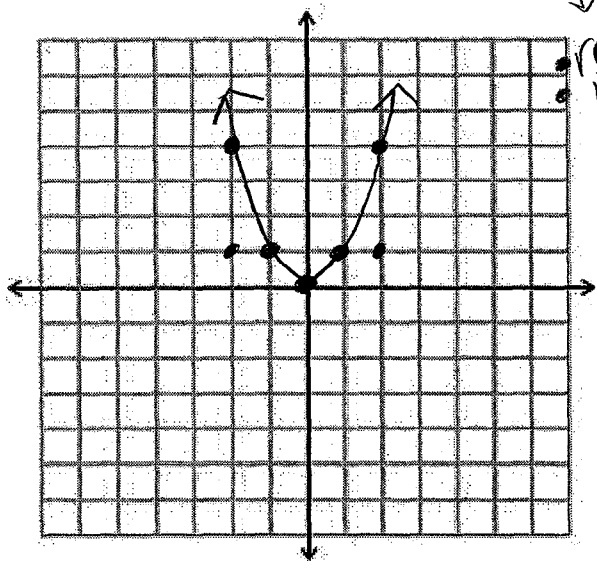
$$1(1-x) - x^2(1-x)$$

$$(1-x^2)(1-x)$$

$$(1+x)(1-x)(1-x)$$

7.

The graph of  $g(x)$  is given below. Graph  $y=g(-2x)$  on the same axes.



(-1, 1)

reflect over y-axis  
horiz. shrink by  $\frac{1}{2}$

~~SKIP~~

8. Write the equation of the line that passes through the points  $(-4, 4)$  and  $(2, -1)$  in **POINT-SLOPE FORM**.

$$m = \frac{4 - (-1)}{-4 - 2} = \frac{5}{-6}$$

$$y - 4 = -\frac{5}{6}(x + 4)$$

OR

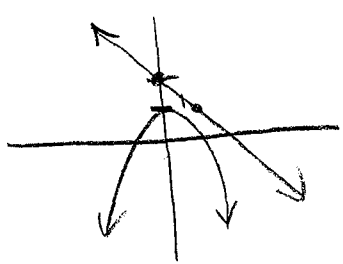
$$y + 1 = -\frac{5}{6}(x - 2)$$

9. Which equation has imaginary roots?

- 1)  $x^2 - 2x + 1 = 0$
- 2)  $x^2 - 2x - 1 = 0$
- 3)  $x^2 - 2x + 5 = 0$
- 4)  $x^2 - 2x - 5 = 0$

(3)

10. How many points of intersection does the system  $y = 1 - x^2$  and  $y = 2 - x$  have?



$$1 - x^2 = 2 - x$$

$$-1 + x^2 + x^2 - 1$$


---

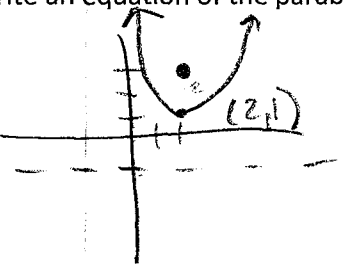

$$0 = x^2 - x + 1$$

0

$$x = \frac{1 \pm \sqrt{1 - 4(1)(1)}}{2} = \frac{1 \pm \sqrt{-3}}{2} \rightarrow \text{imag.}$$

REVIEW # 5

Just solve ... 2 ways!

	Question/WORK	ANSWER
1.	<p><math>p = \frac{c}{a} = -4</math></p> <p>What is the product of the roots of the equation <math>-2x^2 + 3x + 8 = 0</math>?</p> $x = \frac{-3 \pm \sqrt{9 - 4(-2)(8)}}{2(-2)}$ $\frac{(-3 + \sqrt{73})}{-4} \cdot \frac{(-3 - \sqrt{73})}{-4}$	<p>the equation <math>-2x^2 + 3x + 8 = 0</math> ✓</p> $= \frac{-3 \pm \sqrt{73}}{-4}$ $= \frac{9 - 73}{16} = \frac{-64}{16} = -4$
2.	<p>What is the sum of the roots of <math>4x^2 - 5x - 3 = 0</math>?</p> $x = \frac{5 \pm \sqrt{25 - 4(4)(-3)}}{8}$	<p><math>-5x = 3</math> <math>\frac{16}{16}</math></p> $S = \frac{-b}{a} = \frac{5}{4}$ $\frac{5 \pm \sqrt{73}}{8} \rightarrow \frac{5 + \sqrt{73}}{8} + \frac{5 - \sqrt{73}}{8} = \frac{10}{8} = \frac{5}{4}$
3.	<p>Write an equation of the parabola whose focus is (2,3) and directrix is <math>y = -1</math>.</p> 	$y = \frac{1}{4(2)} (x - 2)^2 + 1$ $y = \frac{1}{8} (x - 2)^2 + 1$
4.	<p>Factor: <math>a^6 - a^4 - a^2 + 1</math></p> $a^4(a^2 - 1) - 1(a^2 - 1)$ $(a^4 - 1)(a^2 - 1) = (a^2 + 1)(a^2 - 1)(a + 1)(a - 1)$	$= (a^2 + 1)(a + 1)(a - 1)(a + 1)(a - 1)$
5.	<p>Which equation has imaginary roots?</p> <p><math>b^2 - 4ac</math></p> <p>1) <math>x^2 - 1 = 0</math> <math>0 - 4(1)(-1) = 4 &gt; 0</math></p> <p>2) <math>x^2 - 2 = 0</math> <math>0 - 4(1)(-2) = 8 &gt; 0</math></p> <p>3) <math>x^2 + x + 1 = 0</math> <math>1 - 4(1)(1) = -3 &lt; 0</math> ✓</p> <p>4) <math>x^2 - x - 1 = 0</math> <math>1 - 4(1)(-1) = 5 &gt; 0</math></p>	$= (a^2 + 1)(a + 1)(a - 1)(a + 1)(a - 1)$

6. The mid-September statewide average gas prices, in dollars per gallon, ( $y$ ), for the years since 2000, ( $x$ ), are given in the table below.

Year Since 2000 ( $x$ )	Price Per Gallon ( $y$ )
1	1.345
2	1.408
3	1.537
4	1.58

Write a linear regression equation for this set of data. Using this equation, determine how much *more* the actual 2005 gas price was than the predicted gas price if the actual mid-September gas price for the year 2005 was \$2.956:

$$y = .0834x + 1.259$$

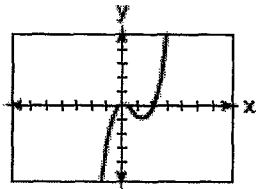
$$y = .0834(5) + 1.259 = 1.676$$

$$2.956$$

$$- 1.676$$

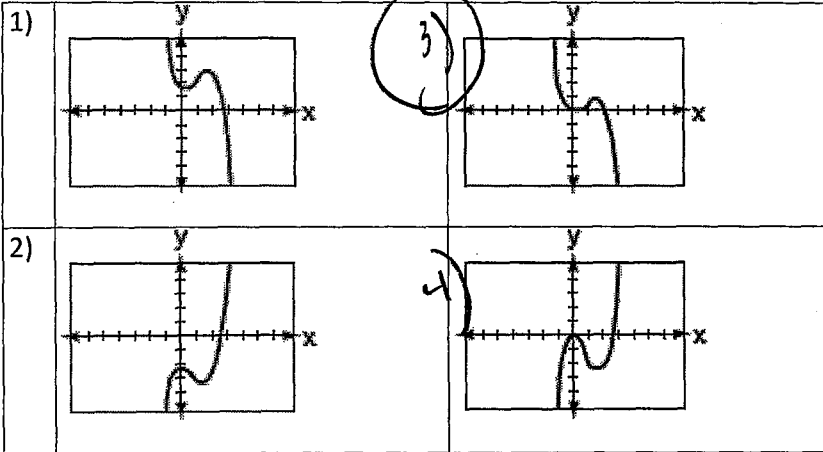
$$\$1.28$$

7. The accompanying graph represents the equation  $y = f(x)$ .



negate  $y \Rightarrow$   
reflect  
in  $x$ -axis

Which graph represents  $g(x)$  if  $g(x) = -f(x)$ ?



(3)

8. Solve and graph your result on a number line:  $2x^2 - 5x - 3 \leq 0$

$$2x^2 - 6x + 1x - 3 = 0$$

$$2x(x-3) + 1(x-3) = 0$$

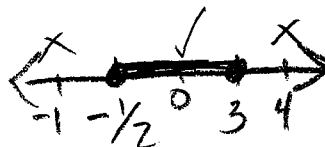
$$(2x+1)(x-3) = 0$$

$$-\frac{1}{2} \quad 3$$

$$ac = -6$$

$$b = -5$$

$$-6 \quad 1$$



$$\left[-\frac{1}{2}, 3\right]$$

9.

State the conjugate of  $9 - \sqrt{11}$ .

$$9 + \sqrt{11}$$

10.

Solve by factoring:  $x^3 + 7x^2 - 7 = 0$ 

*grouping*

$$x^2(x+7) - 1(x-7) = 0$$

*DOTS*

$$(x^2-1)(x+7) = 0$$

$$(x+1)(x-1)(x+7) = 0$$

$$x = \pm 1, -7$$

11.

Solve the system algebraically:

$$x^2 + y^2 = 25$$

$$4x + 3y = 0$$

$$-4x \quad -4y$$

$$\frac{3y}{3} = \frac{-4y}{3}$$

$$x^2 + \left(\frac{-4}{3}x\right)^2 = 25$$

$$\frac{9}{9}x^2 + \frac{16}{9}x^2 = 25$$

$$(9) \frac{25x^2}{9} = 25(9)$$

$$\frac{25x^2}{25} = \frac{225}{25}$$

$$x^2 = 9$$

$$x = \pm 3$$

$$3^2 + y^2 = 25$$

$$y^2 = 16$$

$$y = \pm 4$$

ck:  $4(-3) + 3(4) = 0$

$$4(3) + 3(-4) = 0$$

$$\begin{matrix} (-3, 4) \\ (3, -4) \end{matrix}$$

12.

Find the center and radius of the circle whose equation is

$$x^2 + y^2 - 2x + 4y - 11 = 0$$

$$x^2 - 2x + 1 + y^2 + 4y + 4 = 11 + 1 + 4$$

$$(x-1)^2 + (y+2)^2 = 16$$

$$(x-h)^2 + (y-k)^2 = r^2$$

$$C: (1, -2)$$

$$r = 4$$



# REVIEW # 6

	Question/WORK	ANSWER
1.	Factor Completely: $4x^2 + 4x - 63$ $aC = -252 < 18$ $b = 4 < -14$ $4x^2 + 18x - 14x - 63$ $2x(2x+9) - 7(2x+9)$ $(2x-7)(2x+9)$	
2.	Factor Completely: $x^4 - y^4$ $(x^2 + y^2)(x^2 - y^2)$ $(x^2 + y^2)(x + y)(x - y)$	
3.	Simplify the expression $(x^2 + 1)^2 - 2x^2$ $(x^2 + 1)(x^2 + 1)$ $x^4 + 2x^2 + 1 - 2x^2 = x^4 + 1$	
4.	Solve: $x^3 + 7x^2 - x - 7 = 0$ $x^2(x+7) - 1(x+7) = 0$ $(x+1)(x-1)(x+7) = 0$ $x = -1, 1, -7$	
5.	State the y-intercept of $f(x) = x^2 - 6x + 2$	(0, 2)
6.	Find the sum of the roots of $x^2 - 6x + 2 = 0$ . $S = -\frac{b}{a} = \frac{6}{1}$ $x = \frac{6 \pm \sqrt{36 - 4(1)(2)}}{2} = \frac{6 \pm \sqrt{28}}{2}$	6

$$\frac{6 + \sqrt{28}}{2} + \frac{6 - \sqrt{28}}{2} = \frac{12}{2} = 6$$

$$\frac{c}{a} = \frac{2}{1}$$

7.

Find the product of the roots of  $x^2 - 6x + 2 = 0$ .

$$\frac{(6 + \sqrt{28})}{2} \cdot \frac{(6 - \sqrt{28})}{2} = \frac{36 - 28}{4} = \frac{8}{4}$$

2

8.

Evaluate the discriminant of  $x^2 - 6x + 2 = 0$ .

$$b^2 - 4ac = (-6)^2 - 4(1)(2) = 28$$

28

9.

Solve  $x^2 - 6x + 2 = 0$  by Completing the Square.

$$x^2 - 6x + \frac{9}{2} = -2 + \frac{9}{2}$$

$$\sqrt{(x-3)^2} = \sqrt{7}$$

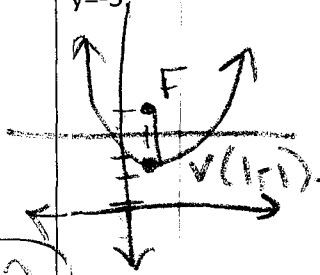
$$x-3 = \pm\sqrt{7}$$

$$x = 3 \pm \sqrt{7}$$

$x = 3 \pm \sqrt{7}$

10.

Write an equation of a parabola which the focus point is (1,1) and directrix is  $y = -3$ .



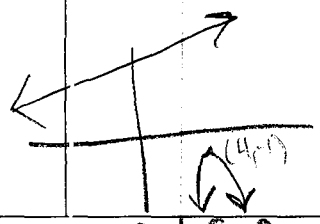
$$y = \frac{1}{4p} (x-h)^2 + k$$

$$y = \frac{1}{8} (x-1)^2 - 1$$

$p=2$

11.

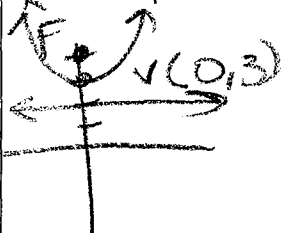
Write a system of two equations in two variables where one equation is quadratic and the other is linear such that the system has no solution. Explain, using graphs, algebra, and/or words, why the system has no solution.



$$y = \frac{1}{2}x + 5$$

$$y = -(x-4)^2 - 1$$

NO INTERSECTION

	Question/WORK	ANSWER
1.	<p>Divide using long division: <math>(x^3 + 3x^2 - x - 8) \div (x - 1)</math></p> $  \begin{array}{r}  x^2 + 4x + 3 \quad R-5 \\  x-1 \overline{) x^3 + 3x^2 - x - 8} \\  \underline{-(x^3 - x^2)} \phantom{-8} \\  4x^2 - x \phantom{-8} \\  \underline{-(4x^2 - 4x)} \phantom{-8} \\  3x - 8 \\  \underline{-(3x - 3)} \\  -5  \end{array}  $	
2.	<p>Explain why <math>(x-1)</math> is or is not a linear factor of <math>(x^3 + 3x^2 - x - 8)</math>.</p> <p>Not a factor b/c there's a remainder</p>	
3.	<p>Write an equation of the parabola whose focus is <math>(0,4)</math> and directrix is <math>y=2</math>.</p>  <p><math>y = \frac{1}{4}x^2 + 3</math></p>	
4.	<p>Write <math>(5 + 2yi)(4 - 3i) - (5 - 2yi)(4 - 3i)</math> in <math>a + bi</math> form, where <math>y</math> is a real number.</p> $  (4-3i)[(5+2yi) - (5-2yi)]  $ $  (4-3i)[8+2yi-5+2yi] = (4-3i)(4yi)  $	$  \begin{array}{l}  16yi - 12yi^2 \\  \hline  16yi + 12y  \end{array}  $

5.	<p>Show that <math>x-4</math> is a factor of the function <math>f(x) = 2x^3 - 5x^2 - 11x - 4</math>. Explain your answer.</p>	
6.	<p>A stadium has 49,000 seats. Seats are priced for \$25 in Section A, \$20 in section B, and \$15 in section C. The number of seats in section A equals the total number of seats in sections B and C. Suppose the stadium takes in \$1,052,000 from each sold-out event. How many seats does each section hold?</p>	<p><math>A = B + C</math>  <math>C = A - B</math>  <math>C = (24,500 - B)</math></p>
7.	<p>Find the axis of symmetry of <math>f(x) = 3x^2 - 6x + 5</math>.</p>	
8.	<p>If <math>\sqrt[3]{(x+1)^5} = (x+1)^a</math>, for <math>x \neq -1</math> and <math>a</math> is a constant, what is the value of <math>a</math>?</p>	

$$\begin{array}{r}
 4 \overline{) 2x^3 - 5x^2 - 11x - 4} \\
 \underline{4x^3 - 16x^2 + 64x - 256} \\
 23x^2 - 75x + 252 \\
 \underline{23x^2 - 92x + 364} \\
 16x - 112 \\
 \underline{16x - 64} \\
 -48
 \end{array}$$

→ remainder

$$\begin{aligned}
 25(24500) + 20B + 15(24500 - B) &= 1,052,000 \\
 612500 + 20B + 367500 - 15B &= 1,052,000 \\
 980,000 + 5B &= 1,052,000 \\
 5B &= 72,000 \\
 \boxed{B = 14,400}
 \end{aligned}$$

A: \$25  
 B: \$20  
 C: \$15

$A = B + C$

$24500 = 14,400 + C$

$\boxed{C = 10,100}$

$$\begin{aligned}
 A + B + C &= 49,000 \\
 A &= B + C \\
 25A + 20B + 15C &= 1,052,000 \\
 B + C + B + C &= 49,000 \\
 2B + 2C &= 49,000 \\
 -2B & \\
 \hline
 2C &= 49,000 - 2B \\
 C &= 24,500 - B
 \end{aligned}$$

$$\begin{aligned}
 A &= B + 24,500 - B \\
 \boxed{A} &= 24,500
 \end{aligned}$$

$$x = \frac{-b}{2a} \Rightarrow \boxed{x = 1}$$

P/R  
2

$$\begin{aligned}
 &\sqrt{(x+1)^{5/3}} \\
 &= \left( (x+1)^{5/3} \right)^{1/2} \\
 &= (x+1)^{5/6} = (x+1)^a
 \end{aligned}$$

$\boxed{a = 5/6}$

$$(x+1)^{5/6} = (x+1)^a$$

## Question/WORK

## ANSWER

1.

$$\begin{aligned} 4x - 2y + 6z &= 10 \\ \text{Solve the system: } 4(x + 3y + z &= 16) \\ 5y - z &= 19 \end{aligned}$$

$$\rightarrow x + 3(4) + 1 = 16$$

$$x + 13 = 16$$

$$\boxed{x = 3}$$

$$\begin{array}{r} 4x - 2y + 6z = 10 \\ + \quad -4x - 12y - 4z = -64 \\ \hline -14y + 2z = -54 \\ 2(5y - z = 19) \\ \hline \end{array}$$

$$\begin{array}{r} -14y + 2z = -54 \\ + \quad 10y - 2z = 38 \\ \hline \end{array}$$

$$-4y = -16$$

$$\boxed{y = 4}$$

$$5(4) - z = 19 \quad \uparrow$$

$$20 - z = 19$$

$$\boxed{z = 1}$$

2.

State the conjugate of  $5 - \sqrt{7}$   $5 + \sqrt{7}$ 

3.

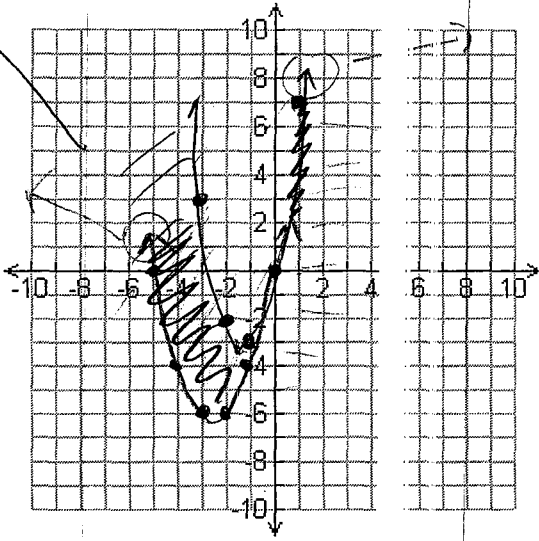
Solve:  $x^2 + 3x - 3 = 0$ 

$$x = \frac{-3 \pm \sqrt{9 - 4(1)(-3)}}{2(1)} = \frac{-3 \pm \sqrt{21}}{2}$$

4.

Solve the system by graphing:

$$\begin{aligned}
 y &= x^2 + 5x & (-2, 0) & \quad 0 > -6 \checkmark \\
 y &= 2x^2 + 5x & (-1, 0) & \quad 0 < -3 \times \\
 & & (-2, -5) & = -3
 \end{aligned}$$



CK on calc (#line)

5.

Factor completely:  $16x^4 - 81y^4$

$$\begin{aligned}
 &(4x^2 - 9y^2)(4x^2 + 9y^2) \\
 &(2x + 3y)(2x - 3y)(4x^2 + 9y^2)
 \end{aligned}$$

6.

Identify the axis of symmetry, vertex, the maximum or minimum value, AND the range of  $y = x^2 + 8x + 18$ .

$$x = \frac{-8}{2(1)} \Rightarrow \boxed{x: -4}$$

$$\boxed{R: y \geq 2}$$

$$\begin{aligned}
 y &= (-4)^2 + 8(-4) + 18 \\
 &= 16 - 32 + 18 = 2
 \end{aligned}$$

$$\boxed{(-4, 2)} \text{ min}$$

7. Find an equation in the form  $y = ax^2 + bx + c$  that goes through the points (4,89), (-1,19), and (-2,53).

~~$x \ y$~~   ~~$x \ y$~~   ~~$x \ y$~~

$$89 = 16a + 4b + c$$

$$* (19 = 1a - 1b + c) - 1$$

$$53 = 4a - 2b + c$$

$$5(34 = 3a - b)$$

$$170 = 15a - 5b$$

$$+ 70 = 15a + 5b$$


---


$$240 = 30a$$

$$19 = 8 + 10 + c$$

$$19 = 18 + c$$

$$c = 1$$

$$+ \begin{array}{r} 89 = 16a + 4b + c \\ -19 = 1a - 1b - c \\ \hline 70 = 15a + 5b \end{array}$$

$$a = 8$$

$$34 = 3(8) - b$$

$$34 = 24 - b$$

$$-24 \quad -24$$


---


$$10 = -b$$

$$+ \begin{array}{r} 53 = 4a - 2b + c \\ -19 = -1a + 1b - c \\ \hline 34 = 3a - b \end{array}$$

$$b = -10$$

8. Show that  $2x + 5$  is a linear factor of  $6x^4 + 15x^3 - 14x^2 - 27x + 20$ . Explain your answer.

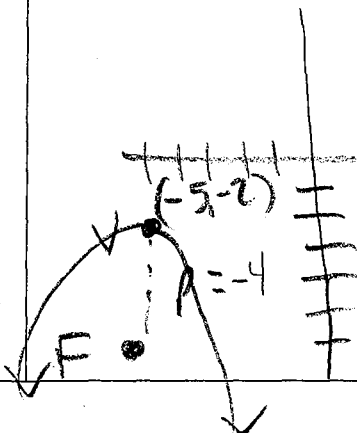
$$\begin{array}{r} \frac{5}{2} \overline{) 6 \ 15 \ -14 \ -27 \ 20} \\ \underline{\downarrow -15 \ 0 \ 35 \ -20} \\ 6 \ 0 \ -14 \ 8 \ 0 = R \end{array}$$

$$\begin{array}{r} 3x^3 + 0x^2 - 7x + 4 \\ \hline 6x^4 + 15x^3 - 14x^2 - 27x + 20 \\ - (6x^4 + 15x^3) \\ \hline 0x^3 - 14x^2 - 27x + 20 \\ - (-14x^2 - 35x) \\ \hline -14x^2 - 27x + 20 \\ - (-14x^2 - 35x) \\ \hline 8x + 20 \end{array}$$

Q:  $3x^3 - 7x + 4$  R: 0

$$\begin{array}{r} 8x + 20 \\ - (8x + 20) \\ \hline 0 \end{array}$$

9. Write an equation of the parabola whose VERTEX is (-5,-2) and FOCUS is (-5,-6)



$$y = \frac{1}{4(-4)}(x+5)^2 - 2$$

$$y = \frac{1}{-16}(x+5)^2 - 2$$

# REVIEW # 9

	Questions/WORK	ANSWER
1.	<p>Which of the following functions decreases as the input values approach both negative infinity and positive infinity?</p> <p>(1) <math>f(x) = x^3 - 4x^2 + x</math>            (2) <math>g(x) = -2x^3 - 4x^2 + 9</math>            (3) <math>h(x) = x^4 - 4x^3 + 2x + 8</math>            (4) <math>r(x) = -x^4 + 9x^3 + x^2 + 8x + 1</math></p>	<p>EB: ↓ ↓            ⊖ even</p>
2.	<p>Which of the following could identify the transformation of a parabola with a vertex of (-4, -6) to parabola with a vertex of (1, -6)?</p> <p>(1) <math>f(x) + 5</math>            (2) <math>5f(x)</math>            (3) <math>f(x + 5)</math>            (4) <math>f(x - 5)</math></p>	<p>right + 5</p>
3.	<p>Someone uses the polynomial identity <math>(x^2 - y^2)^2 + (2xy)^2 = (x^2 + y^2)^2</math> to generate the Pythagorean triple 9, 40, 41. What values of x and y did he use to generate the values for the three sides of a right triangle?</p>	<p><math>x^2 - y^2 = 9</math>  <math>x^2 + y^2 = 41</math>  <math>2xy = 40</math>  <math>x^2 + y^2 = 41</math>  <math>2(5)y = 40</math>  <math>y = 4</math>  <math>x = 5</math></p>
4.	<p>Simplify <math>8i^6 + 6i^5 - 5i^3 - 3i^2 - 7i - 8</math></p>	<p>(calc.)  <math>-14 + 4i</math></p>
5.	<p>Determine the points of intersection for <math>x^2 + y^2 = 1</math> and <math>y = x + 1</math>?</p>	<p><math>2x(x+1) = 0</math>  <math>x = 0</math>   <math>x = -1</math>  <math>y = 1</math>   <math>y = 0</math>  <math>(0, 1)</math>   <math>(-1, 0)</math></p>



6.

Solve  $\sqrt{(x-5)^2} = \sqrt{-9}$

$$x-5 = \pm 3i$$

$$\boxed{x = 5 \pm 3i}$$

7.

A boy standing on the top of an apartment building in Albany throws a water balloon up vertically. The height,  $h$  (in feet), of the water balloon is given by the equation  $h(t) = -16t^2 + 64t + 192$ , where  $t$  is the time (in seconds) after he threw the water balloon. What is the value of  $t$  when the balloon hits the ground? Explain and show how you arrived at your answer.

$$0 = -16t^2 + 64t + 192$$

$$0 = -16(t^2 - 4t - 12)$$

$$(t-6)(t+2) = 0$$

$$\textcircled{t=6} \quad \cancel{t=-2}$$

8.

Divide  $(x^3 + 7x^2 + 14x + 3)$  by  $(x+2)$ . Is  $(x+2)$  a factor of  $(x^3 + 7x^2 + 14x + 3)$ ? Explain why or why not.

$$\begin{array}{r|rrrr}
 -2 & 1 & 7 & 14 & 3 \\
 & \downarrow & -2 & -10 & -8 \\
 \hline
 & 1 & 5 & 4 & \textcircled{-5}
 \end{array}$$

NO, remainder  
is -5

9. Factor completely:  $x^4 - 13x^2 + 36$

$$(x^2 - 9)(x^2 - 4)$$
$$(x+3)(x-3)(x+2)(x-2)$$

10. Solve the system:

$$\begin{array}{r} x+2y-z= \\ + 2x+y+z= \\ - (x+2y+z)= \end{array}$$

$$\begin{array}{r} \rightarrow -x-2y-z=5 \\ + 2x+y+z=0 \end{array}$$

$$\begin{array}{r} x+2y-z=3 \\ + 2x+y+z=0 \end{array}$$

$$\begin{array}{r} 3x+3y=3 \\ -3(x-y=5) \end{array}$$

$$\begin{array}{r} 3y+3y= \\ + -3x+3y=5 \end{array}$$

$$6y=8$$
$$y=3$$

$$3x+3(3)=3$$

$$3x+9=3$$

$$3x=-6$$

$$x=-2$$

$$-2+2(z)-z=3$$

$$-2+z=3$$

$$z=5$$

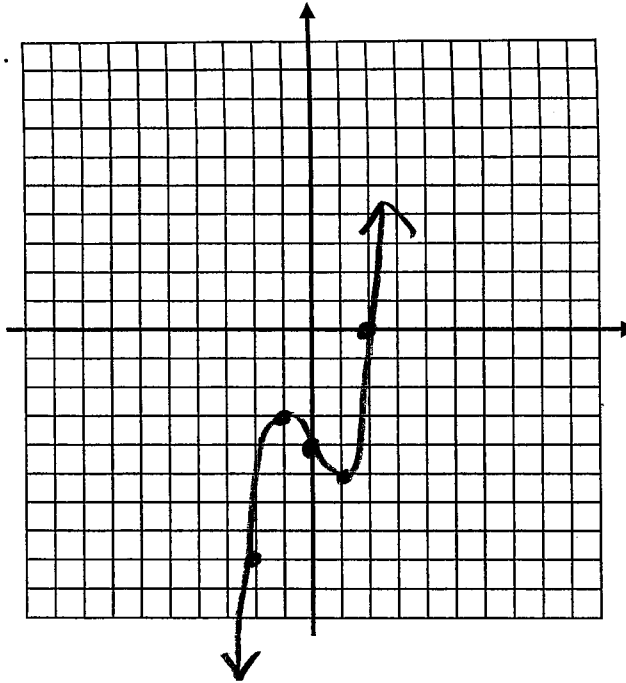
$$z=1$$

$$(-2, 3, 1)$$

11.

Graph  $f(x) = x^3 - 2x - 4$ .

$x$	$y$
-2	-8
-1	-3
0	-4
1	-5
2	0

Based on the graph, what is the real solution to the equation  $x^3 - 2x - 4 = 0$ ?

$$x=2$$

Verify algebraically that it is a zero of  $f(x)$ .

$$f(2) = 2^3 - 2(2) - 4 = 8 - 4 - 4 = 0$$

Write  $f(x)$  as a product of a linear factor and a quadratic factor.

$$2 \begin{array}{r|rrrr} 1 & 1 & 0 & -2 & -4 \\ & \downarrow & 2 & 4 & 4 \\ \hline & 1 & 2 & 2 & 0 \end{array} \quad (x^2 + 2x + 2)(x - 2)$$

Find the two complex number zeros of  $f(x)$ .

$$x^2 + 2x + 2 = 0$$

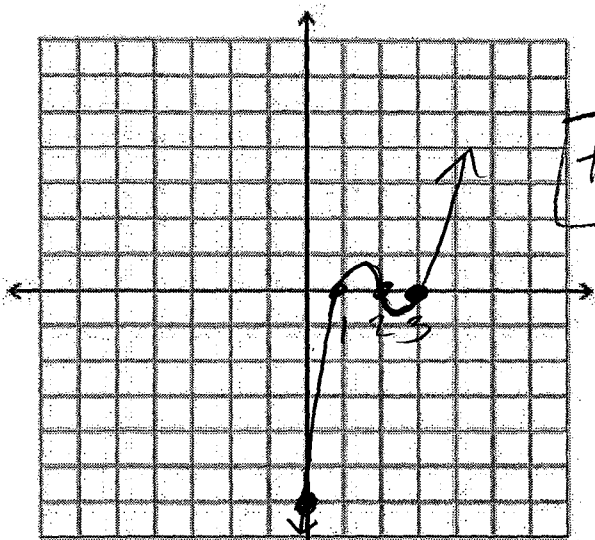
$$x = \frac{-2 \pm \sqrt{2^2 - 4(1)(2)}}{2(1)} = \frac{-2 \pm \sqrt{4 - 8}}{2} = \frac{-2 \pm \sqrt{-4}}{2} = \frac{-2 \pm 2i}{2}$$

$$x = -1 \pm i$$

# REVIEW # 10

	Question/WORK	ANSWER																				
1.	Solve: $(-\sqrt{x+10})^2 = (-7)^2$ $x+10=49$ $x=39$																					
2.	Which equation has non-real solutions? (1) $2x^2 + 4x - 12 = 0$ (2) $2x^2 + 3x = 4x + 12$ (3) $2x^2 + 4x + 12 = 0$ (4) $2x^2 + 4x = 0$																					
3.	Solve: $2x^2 - x + 1 = 0$ $x = \frac{1 \pm \sqrt{1 - 4(2)(1)}}{2(2)}$	$\frac{1 \pm \sqrt{-7}}{4}$ $\frac{1 \pm i\sqrt{7}}{4}$																				
4.	Find a polynomial function of degree 3 in standard form which has the corresponding table of values: $y = x^3 - 2x^2 - 5x - 6$	cubic <table border="1"> <thead> <tr> <th>X</th> <th>Y</th> </tr> </thead> <tbody> <tr><td>4</td><td>18</td></tr> <tr><td>3</td><td>0</td></tr> <tr><td>2</td><td>-4</td></tr> <tr><td>1</td><td>0</td></tr> <tr><td>0</td><td>6</td></tr> <tr><td>-1</td><td>8</td></tr> <tr><td>-2</td><td>0</td></tr> <tr><td>-3</td><td>-24</td></tr> <tr><td>-4</td><td>-70</td></tr> </tbody> </table>	X	Y	4	18	3	0	2	-4	1	0	0	6	-1	8	-2	0	-3	-24	-4	-70
X	Y																					
4	18																					
3	0																					
2	-4																					
1	0																					
0	6																					
-1	8																					
-2	0																					
-3	-24																					
-4	-70																					

5. Use the graph of  $f(x) = x^3 - 6x^2 + 11x - 6$  to rewrite  $f(x)$  as a product of linear factors.



$$f(x) = (x-1)(x-2)(x-3)$$

6. Write  $-4\sqrt{-48}$  in simplest form.

$$-4 \cdot 4i\sqrt{3} = -16i\sqrt{3}$$

7. Write  $n^{\frac{7}{6}}$  in simplest radical form.

$$\sqrt[6]{n^7} = \sqrt[6]{n^6} \cdot \sqrt[6]{n} = n\sqrt[6]{n}$$

8. If  $h(x) = \frac{x-4}{x+5}$ , find  $h^{-1}(x)$ . inverse

$$x = \frac{y-4}{y+5}$$

$$x(y+5) = y-4$$

$$xy + 5x = y - 4$$

$$-xy$$

$$-xy$$

$$5x = y - 4 - xy$$

$$+4$$

$$+4$$

$$\frac{5x+4}{1-x} = \frac{y-xy}{y-4-x}$$

9.

Solve:  $\left[ \frac{4x}{x-3} = 8 + \frac{12}{x-3} \right] (x-3)$

$$4x = 8(x-3) + \frac{12}{1}$$

$$4x = 8x - 24 + 12$$

$$4x = 8x - 12$$

$$-8x - 8x$$

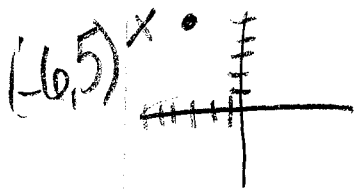
$$\underline{-4x = -12}$$

$$x = 3 \rightarrow$$

add to reject /  
makes denom = 0  
+ fraction undefined

10.

The vertex of a parabola,  $f(x)$  has coordinates  $(-3, 5)$ . Determine the coordinates of the vertex of the parabola defined by  $f(x+3)$ .



left 3

11.

Solve the system:

$$\begin{cases} -2(x-2y+3z) = 7 \\ 2x+y-z = 4 \\ -3x+2y-2z = -10 \end{cases}$$

$$-2x + 4y - 6z = -14$$

$$+ 2x + y - z = 4$$

$$\underline{4(5y - 5z = -10)}$$

$$+ 3x - 6y + 9z = 21$$

$$- 3x + 2y - 2z = -10$$

$$\underline{5(4y + 7z = 11)}$$

$$\begin{aligned} + 20y - 20z &= -40 \\ - 20y + 35z &= 55 \end{aligned}$$

$$\underline{15z = 15}$$

$$z = 1$$

$$5y - 5(1) = -10$$

$$5y = -5 \quad y = -1$$

$$x - 2(-1) + 3(1) = 7$$

$$x + 5 = 7$$

$$x = 2$$

REVIEW # 11

Question/WORK	ANSWER
<p>1. The polynomial <math>p(x) = 2x^3 + 13x^2 + 17x - 12</math> has <math>(x + 4)</math> as a factor.</p> <p>(a) Factor the polynomial into three linear terms.</p> $  \begin{array}{r rrrr}  -4 & 2 & 13 & 17 & -12 \\  & \downarrow & -8 & -20 & 12 \\  \hline  & 2 & 5 & -3 & 0  \end{array}  $ $2x^2 + 5x - 3$ <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>(2x - 1)(x + 3)(x + 4)</math> </div> <p>(b) Describe the steps you would use to sketch the graph of the function (without a calculator). Identify all intercepts and describe the end behavior of the graph.</p> <p>X-ints/roots: <math>x = \frac{1}{2}, -3, -4</math></p> <p>Y-int: <math>(0, -12)</math></p> <p>EB: <math>\downarrow \uparrow</math></p>	
<p>2. Given: <math>f(x) = x^2 - 4x</math>.</p> <p>(a) Write an expression that defines <math>f(x+5)</math>.</p> $  \begin{aligned}  f(x+5) &= (x+5)^2 - 4(x+5) \\  &= x^2 + 10x + 25 - 4x - 20 \\  &= x^2 + 6x + 5  \end{aligned}  $ <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>x^2 + 6x + 5</math> </div> <p>(b) Describe the transformation that maps the graph of <math>f(x)</math> to <math>f(x+5)</math>.</p> <p style="text-align: right;">left 5</p>	

3. State the period of the graph of  $f(x) = -3\cos(2x + \frac{\pi}{2}) - 1$ .

$$f(x) = -3\cos 2(x + \frac{\pi}{4}) - 1$$

$$\text{per} = \frac{2\pi}{b} = \frac{2\pi}{2} = \pi$$

4. Given the two functions  $f(x) = 2x^2 - 4x + 2$ ,  $g(x) = 3 - 3x$ , simplify  $2f(1-x) - 3g(x)$

$$f(1-x) = (1-x)^2 = 2(1 - 2x + x^2)$$

$$= 2 - 4x + 2x^2$$

$$3g(x) = 3(3 - 3x) = 9 - 9x$$

$$2x^2 - 4x + 2 - (-3x + 9)$$

$$2x^2 - 4x + 2 + 3x - 9$$

$$2x^2 - x - 7$$

5. Factor completely:  $162x^4 - 72x^2 + 32$

$$ac = 5184 \quad -72$$

$$b = -144 \quad -72$$

$$162x^4 - 72x^2 + 32$$

$$18x^2(9x^2 - 4) - 8(9x^2 - 4)$$

$$2(9x^2 - 4)(9x^2 - 4)$$

6. Write a quadratic equation in which the sum of the roots is -3 and product of the roots is 5.

$$S = -\frac{b}{a} = -3$$

$$P = \frac{c}{a} = 5$$

$$a = 1$$

$$b = 3$$

$$c = 5$$

$$x^2 + 3x + 5 = 0$$

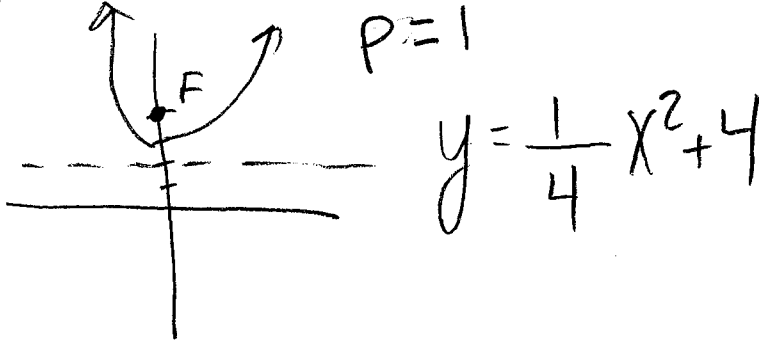


7.

Simplify  $\frac{2(\sqrt{m})^3}{\sqrt[4]{m}}$  and write your answer with a fraction exponent.

8.

Write an equation that represents a parabola with a focus of (0,4) and directrix of  $y=2$ ?



9.

Solve:  $n = \log_{27} 3$

10.

If  $\sqrt[3]{\sqrt{(x+1)^5}} = (x+1)^a$ , for  $x \geq -1$  and  $a$  is constant, what is the value of  $a$ ?

REVIEW # 12

	Question/WORK	ANSWER
1.	For the function $f(x) = (x-3)^{-1} + 1$ , find $f^{-1}(x)$ .	
2.	Factor: $(2a-1)^3 + 8$ $(2a-1)(2a-1)$ $(4a^2 - 4a + 1)(2a-1)$ $8a^3 - 4a^2 - 8a + 4a + 2a - 1 + 8$ $8a^3 - 2a^2 + 6a + 7$	
3.	State the sum and product of the roots of $3x^2 - 5x + 6 = 0$ $x = \frac{5 \pm \sqrt{25 - 4(3)(6)}}{6} = \frac{5 \pm \sqrt{-47}}{6} = \frac{5 \pm i\sqrt{47}}{6}$	
4.	FACTOR COMPLETELY: $k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$ $k^2(k^2 - 4) + 8k(k^2 - 4) + 12(k^2 - 4)$ $(k^2 + 8k + 12)(k^2 - 4)$ $(k+6)(k+2)(k+2)(k-2)$	<i>(Hint: If we factor by grouping with 4 terms ... how about we factor by "chunking" with 6 ... break it into 3 groups of 2. See structure in expressions ... this is on the newly released sample test for Algebra 2. You need to be willing &amp; able to think outside of the box!)</i>

5. Rewrite the expression  $(4x^2 + 5x)^2 - 5(4x^2 + 5x) - 6$  as a product of four linear factors.

(Again - see the structure in expressions - can you see this as  $x^2 - 5x - 6$ ? How does that factor?)

$$(x-6)(x+1)$$

$$(4x^2 + 5x - 6)(4x^2 + 5x + 1)$$

$ac = -24$   
 $b = 5$   
 $8-3$

$$4x^2 + 8x - 3x - 6$$

$$4x(x+2) - 3(x+2)$$

$$(4x-3)(x+2)$$

$$4x^2 + 4x + 1x + 1$$

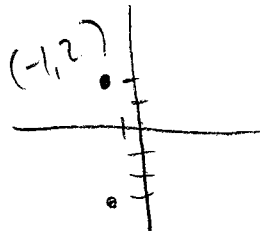
$$4x(x+1) + 1(x+1)$$

$$(4x+1)(x+1)$$

$ac = 4$   
 $b = 5$   
 $1+4$

6. The minimum point on the graph of the equation  $y = f(x)$  is  $(-1, -3)$ . What is the minimum point on the graph of the equation  $y = f(x) + 5$ ?

- 1)  $(-1, 2)$
- 2)  $(-1, -8)$
- 3)  $(4, -3)$
- 4)  $(-6, -3)$

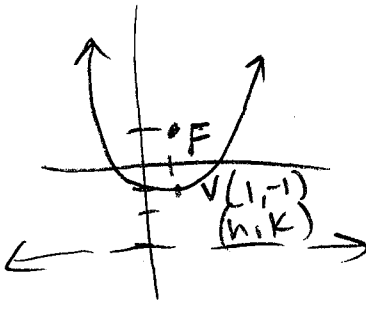


7. Derive the equation of a parabola given the focus of  $(0, 4)$  and the directrix  $y = 2$ .

$$y = \frac{1}{4}x^2 + 4$$

8.	Write an equation of the line, in <u>in-slope form</u> , whose slope is 5 and passes through (-5, 3).	
9.	<p>Factor: <math>6a^2 + 7ax - 3x^2</math></p> <p><math>6a^2 + 9ax - 2ax - 3x^2</math></p> <p><math>3a(2a + 3x) - x(2a + 3x)</math></p> <p><math>(3a - x)(2a + 3x)</math></p> <p><math>ac = -18 \quad a = 9</math> <math>b = 7 \quad c = -2</math></p>	
10.	<p>Solve the system:</p> $\begin{cases} 6x - 2y - 4z = -8 \\ 3x - 5y + 5z = -14 \\ x + y - 5z = 6 \end{cases}$ <p><math>6x - 2y - 4z = -8</math></p> <p><math>-6x + 10y - 10z = 28</math></p> <hr/> <p><math>8y - 14z = 20</math></p> <p><math>8y - 14(-2) = 20</math></p> <p><math>8y + 28 = 20</math></p> <p><math>8y = -8</math></p> <p><math>y = -1</math></p> <p><math>x - 1 - 5(-2) = 6</math></p> <p><math>x - 1 + 10 = 6</math></p> <p><math>x + 9 = 6</math></p> <p><math>x = -3</math></p>	<p><math>3x - 5y + 5z = -14</math></p> <p><math>-3x - 3y + 5z = -18</math></p> <hr/> <p><math>-8y + 20z = -32</math></p> <p><math>+ 8y - 14z = 20</math></p> <hr/> <p><math>6z = -12</math></p> <p><math>z = -2</math></p>

# REVIEW # 13

	Question/WORK	ANSWER
1.	<p>Write a quadratic equation in which the roots are <math>2+i</math> and <math>2-i</math>.</p> $(x - (2+i))(x - (2-i))$ $((x-2)-i)((x-2)+i) \quad \text{FOIL}$ $(x-2)^2 - i^2(-1)$ $x^2 - 4x + 4 + 1 = x^2 - 4x + 5$	
2.	<p>Graph the function <math>f(x) = 3 \cos(2x) + 1</math> between <math>0</math> and <math>2\pi</math>.</p>	
3.	<p>State the EXACT value of <math>\sec \frac{5\pi}{6}</math></p>	
4.	<p>Consider the parabola with focus point <math>(1, 1)</math> and directrix the horizontal line <math>y = -3</math>. Find the equation of the parabola.</p> $y = \frac{1}{8}(x-1)^2 - 1$  <p style="text-align: center;"><math>p=2</math></p>	

# diff. of cubes - SOAP

5. Factor completely:  $\sqrt[3]{(2n-1)^3 - 27}$

$(2n-1) - 3$   
 $2n-1-3$   
 $(2n-4)$

$(2n-1)(2n-1)$   
 $((2n-1)^2 + 3(2n-1) + 3^2)$   
 $(4n^2 - 4n + 1 + 6n - 3 + 9)$   
 $(4n^2 + 2n + 7)$

6. Write an equation of the line, in point-slope form, that goes through (5, 2) and (2, 5)

$m = \frac{5-2}{2-5} = -1$

$y - 2 = -1(x - 5)$

7. The graph of the polynomial function  $f(x) = x^3 + 4x^2 + 6x + 4$  is shown below.

a. Based on the appearance of the graph, what does the real solution to the equation  $x^3 + 4x^2 + 6x + 4 = 0$  appear to be?

$x = -2$

b. Jiju does not trust the accuracy of the graph. Prove to her algebraically that your answer is in fact a zero of  $y = f(x)$ .

$(-2)^3 + 4(-2)^2 + 6(-2) + 4 = 0$   
 $-8 + 16 - 12 + 4 = 0$   
 $8 - 8 = 0$  ✓

c. Find the two complex number zeros of  $x^3 + 4x^2 + 6x + 4 = 0$

$-2 \mid \begin{array}{r} 1 \quad 4 \quad 6 \quad 4 \\ \downarrow -2 \quad -4 \quad -4 \\ \hline 1 \quad 2 \quad 2 \quad 0 \end{array}$

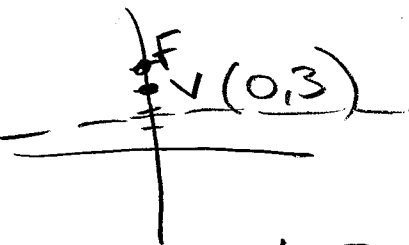
$x^2 + 2x + 2 = 0$

$x = \frac{-2 \pm \sqrt{2^2 - 4(1)(2)}}{2} = \frac{-2 \pm \sqrt{-4}}{2}$

$x = \frac{-2 \pm 2i}{2}$

$x = -1 \pm i$

REVIEW # 14

Question/WORK	ANSWER
<p>1. Write an equation of the parabola with a focus of (0, 4) and a directrix of <math>y=2</math>.</p>  $y = \frac{1}{4}x^2 + 3$	
<p>2. If the terminal side of angle <math>\theta</math>, in standard position, passes through point <math>(-4,3)</math>, what is the exact numerical value of <math>\sin \theta</math>?</p>	
<p>3. Use the properties of rational exponents to determine the value of <math>y</math> in the equation:</p> $\frac{\sqrt[3]{x^8}}{(x^4)^{\frac{1}{3}}} = x^y, x > 1$	

4. Write  $(5+2yi)(4-3i) - (5-2yi)(4-3i)$  in simplest  $a+bi$  form, where  $y$  is a real number.

$$\begin{aligned}
 & 20 - 15i + 8yi - 6y^2 - [20 - 15i - 8yi + 6y^2] \\
 & 20 - 15i + 8yi + 16y^2 - 20 + 15i + 8yi + 6y^2 \\
 & 16yi + 12y^2 \\
 & \boxed{12y^2 + 16yi}
 \end{aligned}$$

5. Use an appropriate procedure to show that  $x-4$  is a factor of the function  $f(x) = 2x^3 - 5x^2 - 11x - 4$ . Explain your answer.

$$\begin{array}{r|rrrr}
 4 & 2 & -5 & -11 & -4 \\
 & \downarrow & 8 & 12 & 4 \\
 \hline
 & 2 & 3 & 1 & 0
 \end{array}$$

Since there is no remainder when dividing by 4,  $(x-4)$  is a factor.

6. Solve algebraically for all values of  $x$ :

$$\sqrt{x-1} + x = 7$$

MT  
Stops here



7. The ocean tides near Carter Beach follow a repeating pattern over time, with the amount of time between each low and high tide remaining relatively constant. On a certain day, low tide occurred at 8:30 a.m. and high tide occurred at 3:00 p.m. At high tide, the water level was 12 inches above the average local sea level; at low tide it was 12 inches below the average local sea level. Assume that high tide and low tide are the maximum and minimum water levels each day, respectively.

Write a cosine function of the form  $f(t) = A \cos(Bt)$ , where  $A$  and  $B$  are real numbers, that models the water level,  $f(t)$ , in inches above or below the average Carter Beach sea level, as a function of the time measured in  $t$  hours since 8:30 a.m.

Graph one cycle of this function.

People who fish in Carter Beach know that a certain species of fish is most plentiful when the water level is increasing. Explain whether you would recommend fishing for this species at 7:30 p.m. or 10:30 p.m. using evidence from the given context.

# REVIEW # 15

	Question/WORK	ANSWER
1.	Solve for all values of x: $\frac{3x+25}{x+7} - \frac{3}{x}$	
2.	Divide: $\frac{6x^3 + 17x^2 + 10x + 2}{2x + 3}$	
3.	Use your answer to #2 to determine if $2x+3$ is a linear factor of $6x^3 + 17x^2 + 10x + 2$	
4.	Write a quadratic equation whose roots are $2 \pm \sqrt{3}$ .	

5.

Solve:  $-\frac{1}{2}x^2 = -6x + 20$

6.

Factor completely:  $n^4 - 4n^2 + 8n^3 - 32n + 12n^2 - 48$

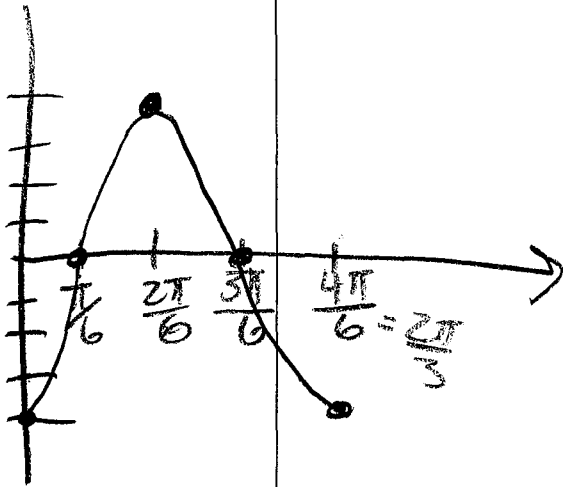
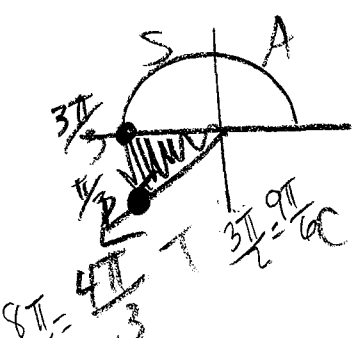
7.

Solve the system algebraically:

$$y = -2x + 1$$
$$y = -2x^2 + 3x + 1$$

8.	Algebraically prove that the difference of the squares of any two consecutive integers is an odd integer.		
9.	<p>Given that <math>x &gt; 0</math>, which expression is equivalent to <math>5\sqrt{xy} + 25\sqrt{x}</math>?</p> <p>(a) <math>5(xy)^{-1} + 25x^{-1}</math></p> <p>(b) <math>25x^{\frac{1}{2}}(\sqrt{y} + 5)</math></p> <p>(c) <math>\sqrt{x}\left(25y^{\frac{1}{2}} + 5\right)</math></p> <p>(d) <math>5x^{\frac{1}{2}}\left(y^{\frac{1}{2}} + 5\right)</math></p>		
10.	Solve: $n = \log_{27} 3$		

# REVIEW # 16

	Question/WORK	ANSWER
1.	<p>If <math>f(x) = 2x^5</math>, find <math>f \circ f^{-1}(-23)</math></p> <p><math>\frac{x = 2y^5}{2} \Rightarrow \sqrt[5]{\frac{x}{2}} = \sqrt[5]{y^5} = y</math></p> <p><math>f^{-1}(-23) = \sqrt[5]{\frac{-23}{2}} = -1.629819719</math></p> <p><math>\boxed{-23}</math></p>	
2.	<p>Graph <math>g(x) = -4 \cos 3x</math></p> <p><math>a = -4</math> / amp = 4</p> <p><math>b = 3</math></p> <p>period = <math>\frac{2\pi}{3}</math></p> <p>x scale = <math>\frac{2\pi}{3} \cdot \frac{1}{4} = \frac{\pi}{6}</math></p> 	
3.	<p>Rewrite <math>\sqrt[5]{x^3}</math> with a rational exponent.</p> <p><math>x^{3/5}</math></p>	
4.	<p>State the exact value of <math>\csc \frac{4\pi}{3}</math></p> <p>Q III</p> <p>R <math>\frac{\pi}{3} = 60^\circ</math></p> <p>F CSC / SIN</p> <p>S -</p>  <p><math>-\sin 60^\circ = -\frac{\sqrt{3}}{2} \Rightarrow \frac{-2 \cdot \sqrt{3}}{2 \cdot \sqrt{3}} = -\frac{2\sqrt{3}}{3}</math></p>	<p><math>\frac{-2\sqrt{3}}{3}</math></p>

5. Two versions of a standardized test are given, an April version and a May version. The statistics for the April version show a mean score of 480 and a standard deviation of 24. The statistics for the May version show a mean score of 510 and a standard deviation of 20. Assume the scores are normally distributed.

(a) Joanne took the April version and scored in the interval 510-540. What is the probability, to the nearest thousandth, that a test paper selected at random from the April version scored in the same interval?



$$\text{Normalcdf}(1.25, 2.5) = \boxed{0.0994}$$

(b) Maria took the May version. In what interval must Maria score to claim she scored as well as Joanne?

$$z = \frac{x - 510}{20} = 1.25$$

$$z = \frac{x - 510}{20} = 2.5$$

$$x - 510 = 25$$

$$x = 535$$

$$x - 510 = 50$$

$$x = 560$$

April

$$\bar{x} = 480$$

$$\sigma = 24$$

May

$$\bar{x} = 510$$

$$\sigma = 20$$

$$\boxed{535-560}$$

6.

Simplify:  $\frac{1}{x-8}$

$$\frac{(x-8) \cdot \frac{1}{x-8}}{(x-8) \cdot \frac{1}{x-8}} = \frac{1}{x-8}$$

$$\frac{x-8-1}{x-8} = \frac{x-9}{x-8}$$

$$= \frac{1}{x-8} \cdot \frac{x-8}{x-9}$$

$$= \boxed{\frac{1}{x-9}}$$

7.

State the midline of  $h(x) = -2 \cos\left(3x - \frac{\pi}{4}\right) + 1$

$$y =$$

8.

$$\begin{aligned} & -3x + 2y - 2z = 10 \\ \text{Solve the system: } & \begin{cases} 6x - 3y - z = 4 \\ -4x + 5y + 2z = 4 \end{cases} \end{aligned}$$

$$\begin{aligned} & -3x + 2y - 2z = 10 \\ + & -12x + 6y + 2z = -8 \\ \hline & -15x + 8y = 2 \end{aligned}$$

$$\begin{aligned} & 12x - 6y - 2z = 8 \\ + & -4x + 5y + 2z = 4 \\ \hline & 8(8x - y = 12) \end{aligned}$$

$$\begin{aligned} & -15x + 8y = 2 \\ + & 64x - 8y = 96 \\ \hline & 49x = 98 \\ & \boxed{x = 2} \end{aligned}$$

$$\begin{aligned} & 8(2) - y = 12 \\ & 16 - y = 12 \\ & \boxed{y = 4} \end{aligned}$$

$$\begin{aligned} & -3(2) + 2(4) - 2z = 10 \\ & -6 + 8 - 2z = 10 \end{aligned}$$

$$\begin{aligned} & 2 - 2z = 10 \\ & \frac{2}{-2} - \frac{2z}{-2} = \frac{10}{-2} \\ & -2z = 8 \\ & \boxed{z = -4} \end{aligned}$$

Sum/diff of cubes:  $x^3 + y^3 = (x+y)(x^2 - xy + y^2)$  AP  
AD

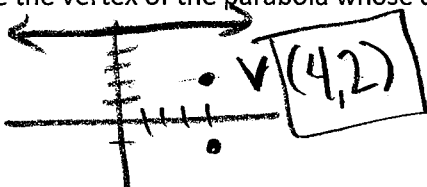
$x^3 - y^3 = (x-y)(x^2 + xy + y^2)$  AD  
AP

9.

Factor:  $64x^3 - 27$ 

$$\begin{aligned} \sqrt[3]{64x^3} &= 4x & (4x-3)((4x)^2 + 3(4x) + 3^2) \\ \sqrt[3]{27} &= 3 & \boxed{(4x-3)(16x^2 + 12x + 9)} \end{aligned}$$

10.

State the vertex of the parabola whose directrix is  $y=5$  and focus is  $(4, -1)$ .

# REVIEW # 17

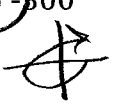
	Question/WORK	ANSWER
1.	<p>Given: <math>h(x) = \frac{2}{9}x^3 + \frac{8}{9}x^2 - \frac{16}{3}x + 2</math></p> <p><math>k(x) = - 0.7x  + 5</math></p> <p>State the solutions to the equation <math>h(x) = k(x)</math>, rounded to the nearest hundredth.</p>	
2.	<p>Find the exact roots of <math>x^2 + 10x - 11 = 0</math> by completing the square.</p>	
3.	<p>Find the difference when <math>\frac{4}{3}x^3 - \frac{5}{8} + \frac{7}{9}x</math> is subtracted from <math>2x^3 + \frac{3}{4}x^2 - \frac{2}{9}</math></p>	



4.	Prove that the equation shown below is an identity for all values for which the functions are defined: $\csc \theta \cdot \sin^2 \theta \cdot \cot \theta = \cos \theta$	
5.	Factor completely: $x^3 + 3x^2 + 2x + 6$	
6.	What is the amplitude of the graph represented by $f(x) = -3\cos \frac{\theta}{3}$ ?	
7.	Solve algebraically for x: $\sqrt{2x+1} + 4 = 8$	

8.	What is the period of the graph represented by $f(x) = -3\cos\frac{\theta}{3}$ ?	
9.	The legs of a right triangle are represented by $x + \sqrt{2}$ and $x - \sqrt{2}$ . Find the exact length of the hypotenuse of the right triangle.	
10.	If $f(x) = 2x^2 - 3x + 4$ , then what is $f(x+3)$ equal to?	
11.	What is the sum of the roots of the equation $-3x^2 + 6x - 2 = 0$ ?	

REVIEW # 18

	Question/WORK	ANSWER
1.	<p>Which angle does <i>not</i> terminate in Quadrant <u>IV</u> when drawn on a unit circle in standard position?</p> <p>(1) <u>-300°</u>      (2) -50°      (3) 280°      (4) 1030°</p> 	
2.	<p>A survey is to be conducted in a small upstate village to determine whether or not local residents should fund construction of a skateboard park by raising taxes. Which segment of the population would provide the most <u>unbiased</u> responses?</p> <p>(1) <del>a club of local skateboard enthusiasts</del>            (2) <del>senior citizens living on fixed incomes</del>            (3) <del>a group opposed to any increase in taxes</del>            (4) <u>every tenth person 18 years of age or older walking down Main St.</u></p>	
3.	<p>Write the expression <math>\frac{\left(\frac{y}{y}\right)^{\frac{1}{x}} + \frac{3\left(\frac{y}{x}\right)}{y}}{\frac{2}{xy}}</math> in simplest form.</p> $\frac{\frac{y+3x}{xy}}{\frac{2}{xy}} = \frac{y+3x}{xy} \cdot \frac{xy}{2} = \boxed{\frac{y+3x}{2}}$	
4.	<p>Rewrite in simplest <u>exponential form</u>: <math>\sqrt[3]{27a^{-6}b^3c^2}</math></p> <p><math>\sqrt[3]{27}</math>      <math>\sqrt[3]{a^{-6}}</math>      <math>\sqrt[3]{b^3}</math>      <math>\sqrt[3]{c^2}</math></p> <p>3      <math>a^{-6/3}</math>      b      <math>\sqrt[3]{c^2}</math></p> <p>         <math>a^{-2}</math></p>	$3a^{-2}b\sqrt[3]{c^2}$

5. Express  $\frac{x}{x-1} - \frac{1}{2-2x}$  as a single fraction in simplest form.

$$\left(\frac{2}{2}\right) \frac{x}{x-1} - \frac{1}{2-2x}$$

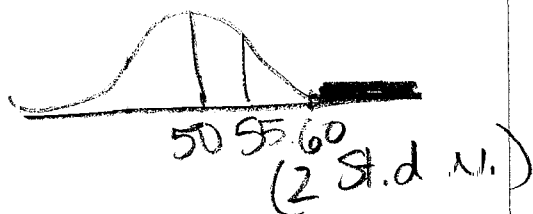
$$\frac{(2x+2) \cdot 2(1-x)}{(2x+2)(2-2x)}$$

$$\frac{-2x-1}{2(1-x)} = \frac{-1(2x+1)}{2-2x}$$

6. What is the product of the roots of the equation  $-3x^2 + 6x - 2 = 0$ ?

$$P = \frac{c}{a} = \frac{-2}{-3} = \boxed{\frac{2}{3}}$$

7. The scores of 1000 students on a standardized test were normally distributed with a mean of 50 and a standard deviation of 5. What is the expected number of students who had scores greater than 60?



$$Z = \frac{60 - 50}{5} = 2$$

$$\text{Normal cdf}(2, 1000) = 0.02275$$

$$\times 1000$$

$$\underline{\hspace{2cm}}$$

$$22.75$$

$\boxed{22}$

8. Find the value of the discriminant of  $4(x^2 - 1) = -3x$ .

$$4x^2 - 4 + 3x = 0$$

$$4x^2 + 3x - 4 = 0$$

$$b^2 - 4ac = 3^2 - 4(4)(-4) = \boxed{73}$$